

Automatic Speech Recognition based on Neural Networks

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Preamble

- joint work with members of HLT & PR lab (Informatik 6):
 - acoustic modeling: Zoltan Tüske, Pavel Golik, Albert Zeyer, Patrick Doetsch, ...
 - language modeling: Martin Sundermeyer, Kazuki Irie, ...
 - cf. hltpr.rwth-aachen.de/web/Publications
- toolkits used for results presented here are available on our web site:
 - RASR: RWTH Automatic Speech Recognition toolkit (also handwriting)
 - RWTHLM: RWTH neural network based Language Modeling toolkit (esp. LSTM)
 - RETURNN: RWTH Extensible Training for Universal Recurrent Neural Networs (new!)
 - ...

- cf. hltpr.rwth-aachen.de/web/Software



Overview

Introduction

Acoustic Modeling

Language Modeling

Sequence Modeling and Search

Specific Work



Introduction

Outline

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Introduction

Sequence Classification

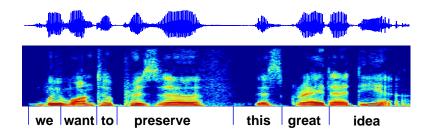
Tasks for machine learning:

- automatic speech recognition
- text image recognition
- machine translation

Most general case:

- input sequence:
 - $X := x_1 \dots x_t \dots x_T$
- output sequence (of unknown length N):
 W := w₁...w_n...w_N
- true distribution pr(W|X)
 (can be extremely complex!)

Speech Recognition



Text Image Recognition

we want to preserve this great idea

Machine Translation

wir wollen diese große Idee erhalten



we want to preserve this great idea



Sequence Decision Rule

- performance measure or loss function $L[\widetilde{W}, W]$ (e.g. edit distance) between true output sequence \widetilde{W} and hypothesized output sequence W.
- Bayes decision rule minimizes expected loss:

$$X \to \overline{W}(X) := \arg\min_{W} \left\{ \sum_{\widetilde{W}} pr(\widetilde{W}|X) \cdot L[\widetilde{W}, W] \right\}$$

• Standard decision rule uses sequence-level loss:

$$X
ightarrow \widehat{W}(X) := rg\max_{W} \left\{ pr(W|X)
ight\}$$

Since [Bahl & Jelinek⁺ 1983], this simplified Bayes decision rule is widely used for speech recognition, handwriting recognition, machine translation, ...

 Works well, as often both decision rules coincide. This can be proven under certain conditions [Schlüter & Nussbaum⁺ 2012], e.g.:

$$L[W, \widetilde{W}]$$
 is a metric, and max $\mathop{pr}(W|X) \geq 0.5 \quad \Rightarrow \quad \overline{W}(X) = \widehat{W}(X)$



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Statistical Approach Revisited

Ingredients:

- **performance measure** (often edit distance):
 - to judge the quality of the system output
- probabilistic models (with a suitable structure):
 - to capture the dependencies within and between X and W
 - elementary observations: Gaussian mixtures, log-linear models, SVMs, NNs, ...
 - strings: n-gram Markov chains, HMMs, CRFs, RNNs, ...

• training criterion:

to learn the free parameters of the models

- ideally should be linked to performance criterion
- might result in complex mathematical optimization (efficient algorithms!)

• Bayes decision rule:

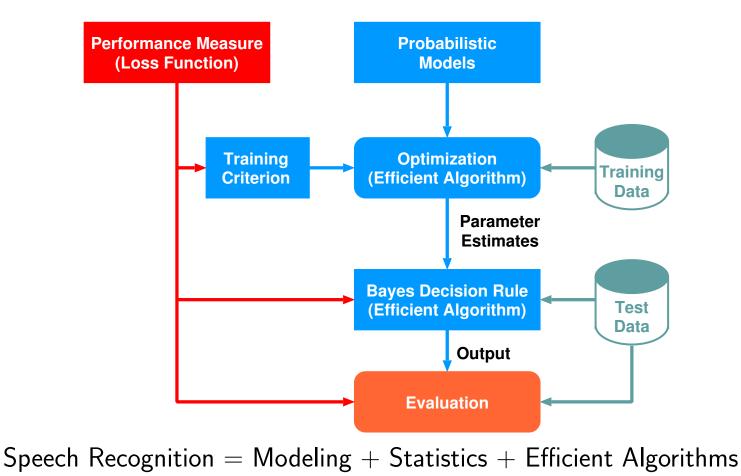
to generate the output word sequence

- combinatorial problem (efficient algorithms)
- should exploit structure of models

Examples: dynamic programming and beam search, A^{\ast} and heuristic search, \ldots



Bayes Architecture for Speech Recognition (and other NLP tasks)





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Sequence Classification

- Problem in Bayes decision rule:
 - true posterior distribution: unknown
 - to replace it, assume suitable model distributions with free parameters:

$$p(W|X) = rac{p(W) \cdot p(X|W)}{\sum_{W'} p(W') \cdot p(X|W')}$$

- generative model: language model p(W) and acoustic model p(X|W)
- Acoustic model p(X|W) provides link between sentence hypothesis W and observation sequence $X = x_1^T = x_1...x_t...x_T$:
 - acoustic probability $p(x_1^T|W)$ using hidden state sequences s_1^T :

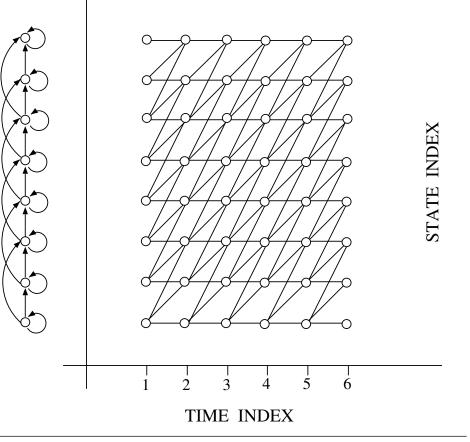
$$p(x_1^T|W) = \sum_{s_1^T} p(x_1^T, s_1^T|W) = \sum_{s_1^T} \prod_t [p(s_t|s_{t-1}, W) \cdot p(x_t|s_t, W)]$$

- two types of distributions:
 - * transition probability p(s|s', W): not important
 - * emission probability $p(x_t|s, W)$: key quantity realized by GMM: Gaussian mixtures models (trained by EM algorithm)



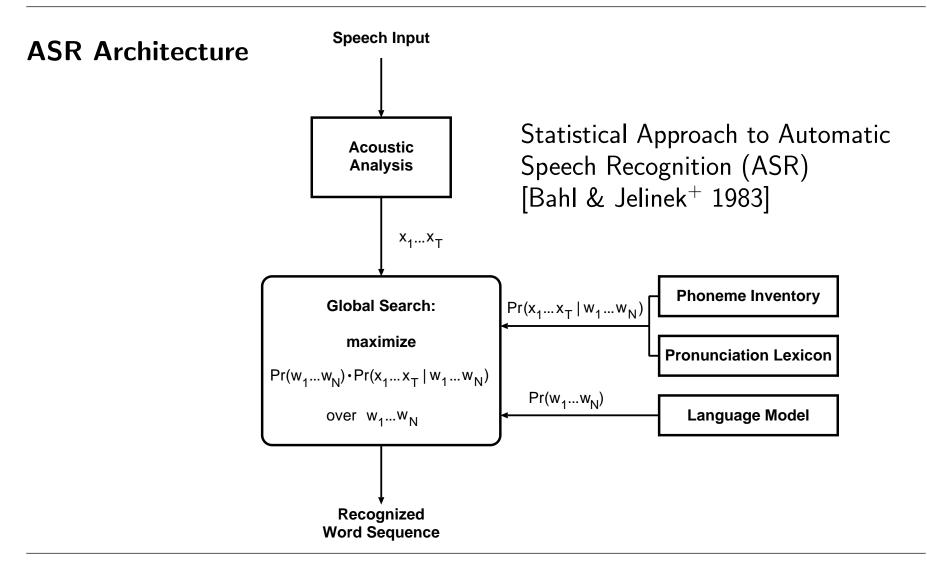
Hidden Markov Models (HMM)

- fundamental problem in ASR: non-linear time alignment
- Hidden Markov Model:
 - linear chain of states s = 1, ..., S
 - transitions: forward, loop and skip
- trellis:
 - unfold HMM over time t = 1, ..., T
 - path: state sequence $s_1^T = s_1...s_t...s_T$
 - observations: $x_1^T = x_1 \dots x_t \dots x_T$





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HMM using Artificial Neural Network Output: Hybrid Approach

consider modeling the acoustic vector x_t in an HMM:

• phonetic labels (allophones, sub-phones): $(s, W) \rightarrow \alpha = \alpha_{sW}$ (typical approach: decision trees, e.g. CART):

$$p(x_t|s, W) = p(x_t|\alpha_{sW})$$

• re-write the emission probability for label α and acoustic vector x_t :

$$p(x_t|\alpha) = \frac{p(x_t) \cdot p(\alpha|x_t)}{p(\alpha)}$$

- prior probability $p(\alpha)$: estimated as relative frequencies (alternatively averaged NN posteriors)
- for recognition purposes: term $p(x_t)$ can be dropped
- result: rather than the state emission distribution $p(x_t|\alpha)$, model the label posterior probability by an NN:

$$x_t \rightarrow p(\alpha | x_t)$$

- justification:
 - easier learning problem: labels $\alpha = 1, ..., 5000$ vs. vectors $x_t \in \mathbb{R}^{D=40}$
 - well-known result in pattern recognition (but ignored in ASR!)



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History: Artificial Neural Networks in Acoustic Modeling

approaches in ASR:

- [Waibel & Hanazawa⁺ 1988]: phoneme recognition using time-delay neural networks
- [Bridle 1989]: softmax operation for probability normalization in output layer
- [Bourlard & Wellekens 1990]:
 - for squared error criterion, NN outputs can be interpreted as class posterior probabilities (rediscovered: Patterson & Womack 1966)
 - they advocated the use of MLP outputs to replace the emission probabilities in HMMs
- [Robinson 1994]: recurrent neural network
 - competitive results on WSJ task
 - his work remained a singularity in ASR

• ...

experimental situation:

until 2011, NNs were never really competitive with(out) Gaussian Mixture Models



History: Artificial Neural Networks in Acoustic Modeling

related approaches:

- [LeCun & Bengio⁺ 1994]: convolutional neural networks
- A. Waibel's team [Fritsch & Finke⁺ 1997]: hierarchical mixtures of experts
- [Hochreiter & Schmidhuber 1997]: long short-term memory neural computation (LSTM RNN) with extensions [Gers & Schraudolph⁺ 2002]
- (second) renaissance of NN: concepts of deep learning and related ideas:
 - [Hermansky & Ellis⁺ 2000]: tandem approach multiple layers of processing by combining Gaussian model and NN for ASR
 - [Utgoff & Stracuzzi 2002]: many-layered learning for symbolic processing
 - [Hinton & Osindero⁺ 2006]: introduced what they called *deep learning (belief nets)*
 - [Graves & Bunke⁺ 2008]: good results for LSTM RNN on handwriting task
 - Microsoft Research [Seide & Li⁺ 2011, Dahl & Yu⁺ 2012]:
 - combined Hinton's deep learning with hybrid approach
 - significant improvement by deep MLP on a large-scale task
 - since 2012: other teams confirmed reductions of WER by 20% to 30%



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Empirical Overview of Current Methods

Experimental conditions:

• QUAERO task: English broadcast news and conversations (evaluation campaign 2011)

- training data: two conditions: 50 and 250 hours
- test data: dev and eval sets, each 3 hours
- language model: vocabulary size of 150k (OOV: 0.4%) and perplexity of 130

Baseline Gaussian mixture HMM based acoustic model:

- feature vector: 16 MFCC (mel frequency cepstral coefficients)
- augmented feature vector: $9 \cdot 16 = 144$
- high-performance baseline system:

Gaussian mixtures with pooled diagonal covariance matrix:

- reduction by LDA to 45-dimensional vector
- 4501 CART labels
- 680k densities
- total number of free parameters: $680k \cdot (45 + 1) = 31.3M$



Gaussian Mixture Models (GMM): Influence of Training Criteria

Training Criterion	WER [%]			
	50h		250h	
	dev	eval	dev	eval
Maximum likelihood	24.4			
MMI at frame level	23.9	30.9	22.1	28.6
MMI at sentence level	24.1	31.2	21.7	28.1
Minimum phone error	23.6	30.2	20.4	26.2

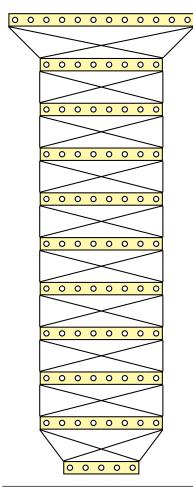
remarks:

- best improvement over maximum likelihood:
 5-10% relative by MPE (Minimum Phone Error)
- comparative evaluations in QUAERO: competitive results with LIMSI Paris and KIT Karlsruhe



Acoustic Modeling

Deep MLP: Number of Hidden Layers



• WER vs. number of hidden layers for 50-h training corpus	hidden WER [%] layers dev eval			
Structure of MLP:	1 1	24.5		
 input dimension: 493 (window + derivatives) 	2	22.0	28.3	
– 2000 nodes per hidden layer	3	20.5	26.7	
 nonlinearity: sigmoid number of parameters for 6-layer MLP: 	4	19.8	26.1	
	5	20.1	26.0	
493 · 2000	6	19.6	25.4	
$+5 \cdot 2000^{2}$	7	19.7	25.5	
$+2000 \cdot 4501 = 30 M$	8	19.6	25.7	
	9	19.3	25.3	
 improvement over best GMM: 20% melating 	best GMM	23.6	30.2	
20% relative				



Practicalities of NN Training: Implementation and Software

typical procedure:

- input data: (sentence-wise) mean and variance normalization
- random initialization of weights: [-0.1,...,+0.1]
- training criterion: (frame-wise) cross-entropy
- stopping: cross-validation on 10% of training data
- sigmoid function
- no regularization, no momentum term, no drop-out (so far!)
- learning rate: reduced over time by a factor of 20-50
- use of minibatches: 512 frames
- pretraining:
 - supervised pretraining: layer by layer
 - in general: not crucial
- use of GPUs: speed-up by a factor of 10 over multithreaded CPUs



Discriminative Sequence Training: MPE vs. CE

Comparison of two training criteria (MLP with 6 hidden layers, 2000 nodes each):

- baseline: cross-entropy = frame MMI
- MPE: minimum phone error (context of pron. lexicon and language model)

Model	Criterion	WER [%]			
INIOUEI	CITTERION	50h		250h	
		dev	eval	dev	eval
MIP	frame MMI	19.6	25.4	15.2	20.4
	MPE	17.5	23.3	14.1	19.2
best GMM		23.6	30.2	20.4	26.4

experimental result: improvement of 5-10% by MPE over frame MMI





Activation Function: Sigmoid vs. RLU

- activation functions:
 - sigmoid function: $u
 ightarrow f(u) = 1/(1 + e^{-u})$
 - RLU=rectified linear unit: $u \rightarrow f(u) = \max\{0, u\}$
- structure of MLP:
 - 6 hidden layers, each with 2000 nodes
 - training condition:
 - * (frame-wise) cross-entropy
 - * L2 regularization (weight decay): important
 - * momentum term
- word error rates for activations functions: sigmoid vs. RLU:

	WER [%]				
activation	50h		250h		
function	dev	eval	dev	eval	
sigmoid	19.6	25.4	15.2	20.4	
RLU	17.7	23.5	14.7	19.6	
best GMM	23.6	30.2	20.4	26.4	
$r_{\rm result}$ in a second of E 100/ by DI					

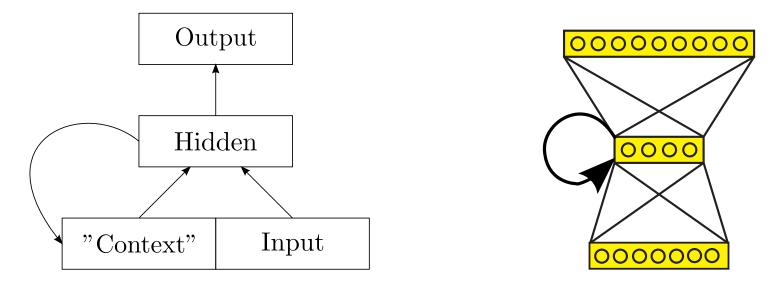
• experimental result: improvement of 5-10% by RLU over sigmoid



Recurrent Neural Network (RNN): Principle

principle:

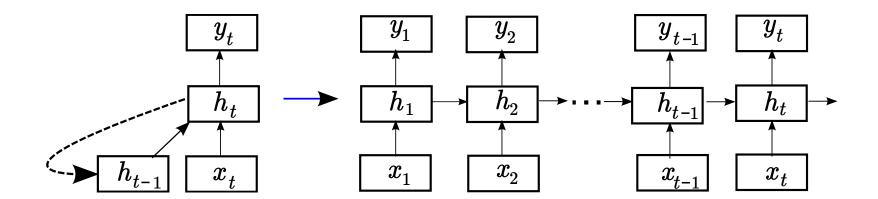
- introduce a **memory** (or context) component to keep track of history
- result: there are two types of input: memory h_{t-1} and observation x_t







Unfolding RNN over Time



The architecture of RNN can be unfolded over time:

- We get a feedforward network with a special **deep** architecture.
- The application of the backpropagation algorithm to this unfolded network is called **backpropagation through time**.

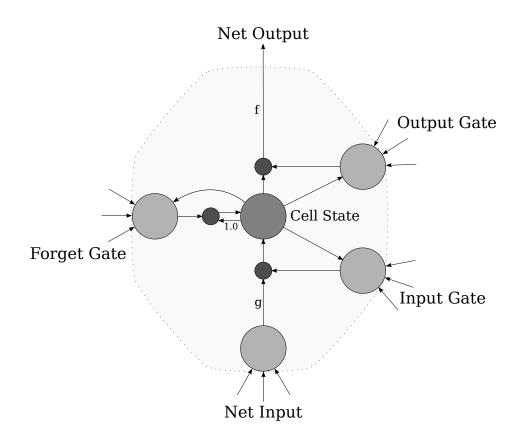


Acoustic Modeling

LSTM RNN [Hochreiter & Schmidhuber 1997, Gers & Schraudolph⁺ 2002]

extension of (simple) RNN by LSTM: long short-term memory

- problems of simple RNN:
 - vanishing/exploding gradients
 - no protection of memory h_t
- remedy by LSTM architecture: control the access to its internal memory by introducing gates/switches
- refinements:
 - bidirectional structure
 - several hidden layers

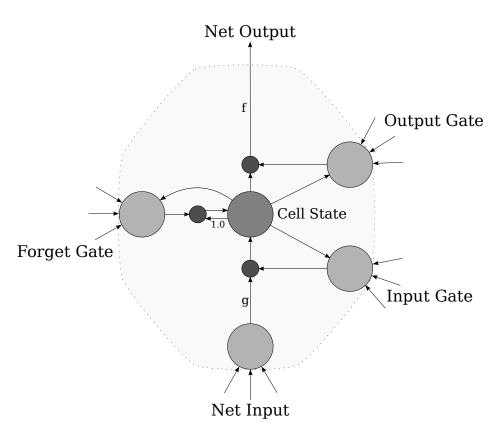




LSTM RNN [Hochreiter & Schmidhuber 1997, Gers & Schraudolph⁺ 2002]

LSTM approach:

- split RNN hidden vector h_t into (memory) cell state c_t and net output s_t
- overall LSTM operations involve three 'input' vectors at time t: s_{t-1}, c_{t-1}, x_t
- update operations at time t: cell state: $c_t = c_t(s_{t-1}, c_{t-1}, x_t)$ net output: $s_t = s_t(s_{t-1}, c_{t-1}, x_t)$ output layer: $y_t = y_t(s_t)$ with softmax
- introduce three gates (input, output, forget) to control the information flow





Acoustic Modeling

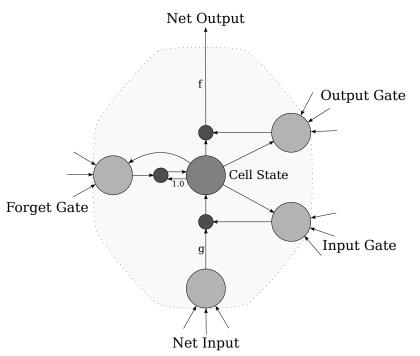
LSTM Architecture

- three vectors (over time t): c_t, s_t, x_t
- gates (or switches): use sigmoid function $\sigma(\cdot)$
- full matrices (A2, R; Ai, Ri, Af, Rf, Ao, Ro) and diagonal matrices (Wi, Wf, Wo)
- usual matrix and vector operations and element-wise multiplication \odot
- Net Input (like update formula of simple RNN):

$$z_t = \tanh(A_2 x_t + R s_{t-1})$$

- Should this Net Input z_t access the Cell State c_t ? Input Gate: $i_t = \sigma(A_i x_t + R_i s_{t-1} + W_i c_{t-1})$
- Should the Cell State c_{t-1} be forgotten? Forget Gate: $f_t = \sigma(A_f x_t + R_f s_{t-1} + W_f c_{t-1})$
- Based on i_t and f_t , update the Cell State c_t : $c_t = f_t \odot c_{t-1} + i_t \odot z_t$
- Should this update c_t be output? Output Gate: $o_t = \sigma(A_o x_t + R_o s_{t-1} + W_o c_t)$
- Based on o_t , compute the Net Output:

$$s_t = o_t \odot c_t$$





Deep LSTM-RNN

50h QUAERO training corpus:

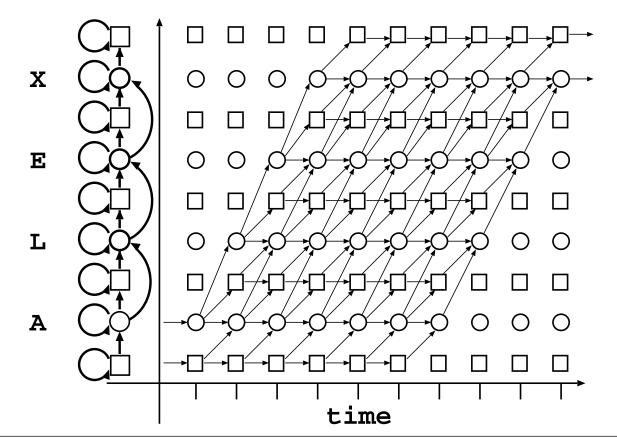
- baseline: best MLP:
 - input: 50 Gammatone features
 - 9 hidden layers
 - RLU
 - training criterion: cross-entropy
- LSTM-RNN structure:
 - input: 50 Gammatone features
 - training criterion: cross-entropy
 - bidirectional with several hidden layers
 - 500 nodes per hidden layer
 - training on a single GPU
- eval improvements:
 - 14% relative over MLP
 - -42% relative over GMM

LSTM	#parame	time /	WEF	R [%]
layers	#params	epoch	dev	eval
1	6.7M	0:28h	17.6	22.7
2	12.7M	1:00h	14.6	18.8
3	18.7M	1:11h	14.0	18.4
4	24.7M	1:33h	13.5	17.7
5	30.7M	1:48h	13.6	17.7
6	36.7M	2:10h	13.5	17.5
7	42.7M	2:36h	13.8	18.0
8	48.7M	3:14h	14.2	18.4
best MLP (9x2000)	42.7M	0:35h	15.3	20.3
best GMM	31.3M	_	23.6	30.2



CTC: Connectionist Temporal Classification

[Graves & Fernández⁺ 2006, Graves & Bunke⁺ 2008]





Related Research Directions

- CTC: What is different from an HMM? What is important?
 - topology: several vs. single state per symbol
 - training criterion: sum vs. maximum
 - no transition probabilities
 - NN structure: RNN-LSTM
- recent neural network approaches (replacing the HMM alignment?):
 - end-to-end approaches
 - mechanism of attention



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Review: Language Modeling

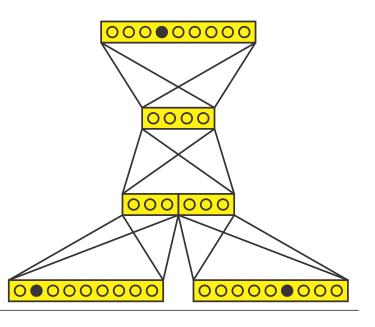
• distinguish:

- *sub-symbolic* processing: speech/audio, text images, image/video (computer vision)
- symbolic processing: language modeling (and machine translation)
- word sequence $w_1^N := w_1 \dots w_n \dots w_N$
- language model: conditional probability $p(w_n|w_0^{n-1})$ (with artificial start symbol w_0):

$$p(w_1^N) = \prod_{n=1}^N p(w_n|w_0^{n-1})$$

- approaches to modeling $p(w_n|w_0^{n-1})$
 - count models (Markov chain):
 - * limit history w_0^{n-1} to k predecessor words
 - * smooth relative frequencies (e.g. SRI toolkit)
 - MLP models:
 - * limit history, too
 - * use predecessor words as input to MLP
 - RNN models: unlimited history!







History of Neural Networks in Language Modeling

• [Nakamura & Shikano 1989]:

English word category prediction based on neural networks.

• [Castano & Vidal⁺ 1993]:

Inference of stochastic regular languages through simple recurrent networks

- [Bengio & Ducharme⁺ 2000]: A neural probabilistic language model
- [Schwenk 2007]:
 - Continuous space language models
- [Mikolov & Karafiat⁺ 2010]: Recurrent neural network based language model
- RWTH Aachen [Sundermeyer & Schlüter⁺ 2012]:
- LSTM recurrent neural networks for language modeling
- RWTH Aachen [Sundermeyer & Tüske⁺ 2014]: long range LM rescoring beyond *N*-best lists

Today: neural network based language models show competitive results.



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Structure of Neural Network for Language Modeling

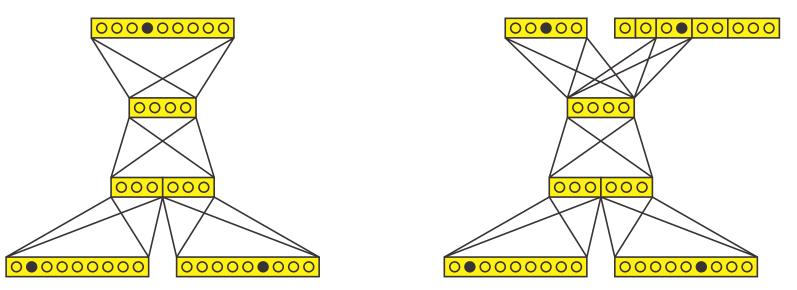
- input layer: k predecessor words with 1-of-V coding (V = vocabulary size)
- first layer: projection layer
 - idea: dimension reduction (e.g. from 150k to 600!)
 - a linear operation (matrix multiplication) without sigmoid activation
 - shared accross all predecessor words of the history h
- output layer:
 - conditional probability of language model p(w|h)
 - softmax operation for normalization
- training criterion:
 - perplexity: equivalent to cross-entropy
 - early stopping using cross-validation on dev corpus
- properties of softmax operation:
 - computationally expensive (sum over full vocabulary)
 - remedy: word classes (automatically trained)
 - normalized outputs of softmax fit nicely into perplexity criterion



Language Modeling

Word Classes

 $\mathsf{MLP}\xspace$ w/o and with Word Classes: Trigram LM



factorization of conditional language model probability p(w|h) for each history h:

$$p(w|h) = p(g|h) \cdot p(w|g,h)$$

using a unique word class g for each word w



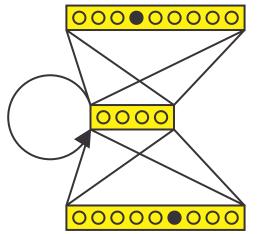
Word Classes

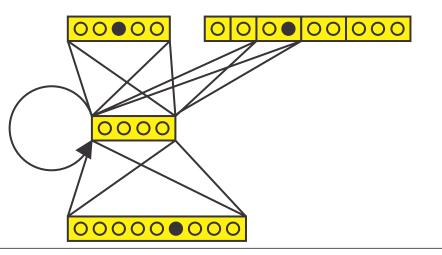
RNN without and with Word Classes

- NN with memory for sequence processing
- left-to-right processing of word sequence $w_1...w_n...w_N$

$$p(w_1^N) = \prod_n p(w_n|w_0^{n-1}) = \prod_n p(w_n|w_{n-1}, h_{n-1})$$

- input to RNN in position *n*:
 - output h_{n-1} of hidden layer at position (n-1)
 - immediate predecessor word w_{n-1}





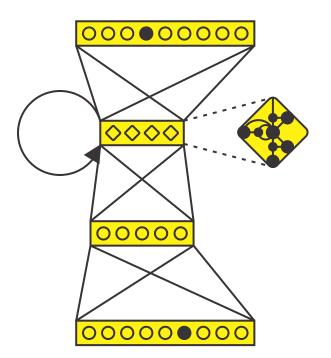


Language Modeling

LSTM RNN [Hochreiter & Schmidhuber 1997, Gers & Schraudolph⁺ 2002]

refinement of RNN: LSTM = long-short term memory

- RNN: problems with vanishing/exploding gradients
- remedy: cells with gates rather than nodes
- details: see literature





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Experiments

- results on QUAERO English (like before):
 - vocabulary size: 150k words
 - training text: 50M words
 - dev and eval sets: 39k and 35k words
- MLP: structure:
 - projection layer: 300 nodes
 - hidden layer: 600 nodes
 - size of MLP is dominated by input and output layers: $150k \cdot 300 + 600 \cdot 150k = 135M$
- RNN (and LSTM RNN): structure
 - projection and hidden layer: each 600 nodes
 - size of RNN is dominated by input and output layers: $150k \cdot 600 + 600 \cdot 150k = 180M$

perplexity PPL on dev data:

approach	hidden	PPL
	layers	
count model	_	163.7
10-gram MLP	1	136.5
	2	130.9
RNN	1	125.2
LSTM-RNN	1	107.8
	2	100.5

observation: (huge) improvement by 40%



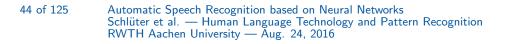
Complexity: Computation Times

Training times (without GPUs!) for training corpus of 50 Million words:

Models	PPL	CPU Time (Order)
Count model	163.7	30 min
MLP	136.5	1 week
LSTM-RNN	107.8	3 weeks

- problem: high computation times
- remedy: two types of language models:
 - count model: trained on a huge corpus: 3.1 Billion words
 - NN models: trained on a small corpus: 50 Million words
- resulting language model:

linear interpolation of two models





Interpolated Language Models: Perplexity and WER

- linear interpolation of *two* models: count model + NN model
- perplexity and word error rate on test data:

Models	PPL	WER[%]
count model	131.2	12.4
+ 10-gram MLP	112.5	11.5
+ Recurrent NN	108.1	11.1
+ LSTM-RNN	96.7	10.8
+ 10-gram MLP with 2 layers	110.2	11.3
+ LSTM-RNN with 2 layers	92.0	10.4

- experimental result:
 - significant improvements by NN language models
 - best improvement in perplexity: 30% reduction (from 131 to 92)
 - empirical observation:

power law between WER and perplexity (cube to square root)



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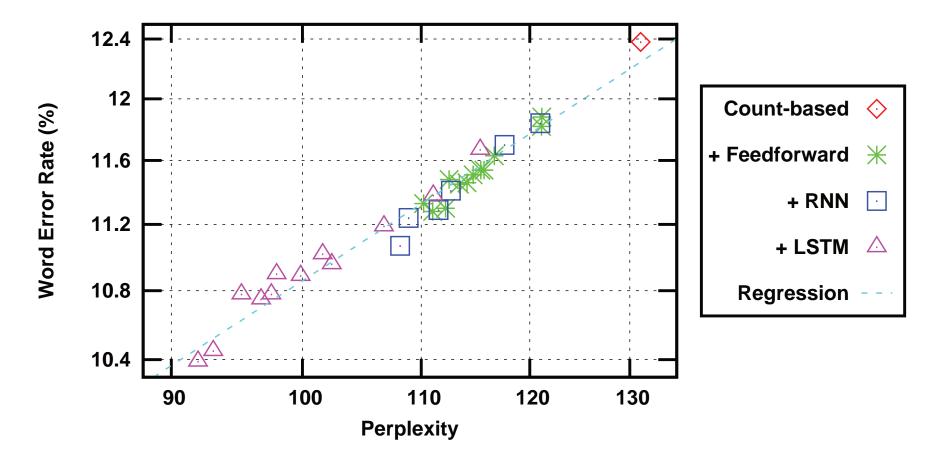
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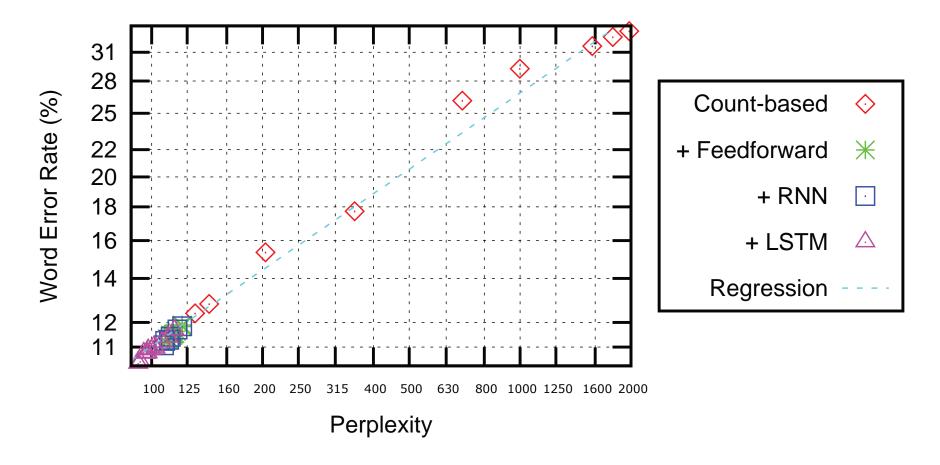
Perplexity vs. Word Error Rate

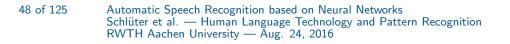




Language Modeling

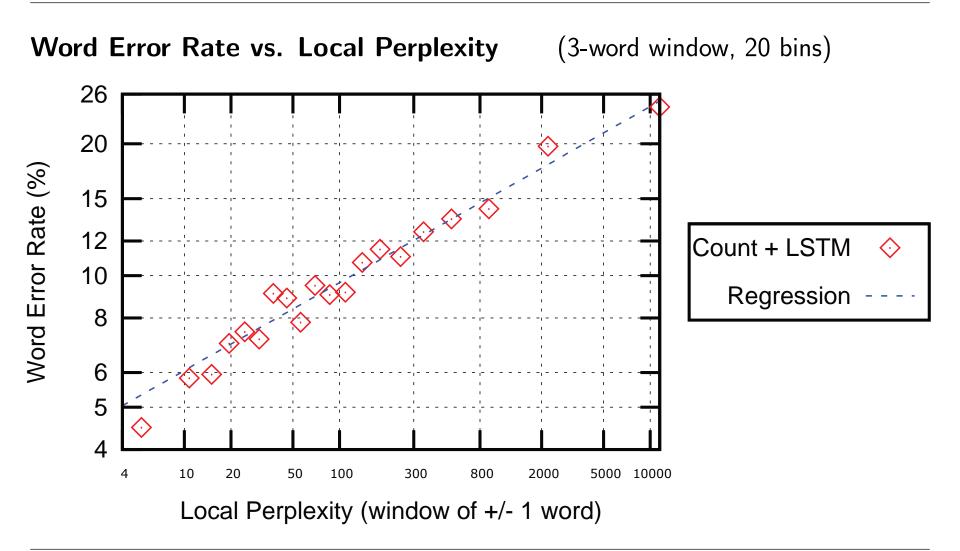
Extended Range: Perplexity vs. Word Error Rate







Language Modeling







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Motivation

- End-to-end model:
 - Consistence of modeling, training, and decoding.
 - Cover segmentation problem by NN structure: sequence length, duration, and positioning of words are unknown.
 - Context dependence needs to be modeled.
- Ultimate goals (not fully achieved yet):
 - Integration of NN models into Bayes decision rule.
 - Separation of acoustic & language model (resources usually differ).
 - Consistence between decision rule, evaluation measure, and training objective.



Sequence Modeling and Search

Review: Hidden Markov Modeling

- $\ {\ }$ models words/word sequences by HMM state sequences
- within Bayes decision rule:

$$\begin{aligned} \arg \max_{N,w_1^N} p(w_1^N) \cdot p(x_1^N | w_1^N) &= \arg \max_{N,w_1^N} p(w_1^N) \cdot \sum_{s_1^T : w_1^N} p(x_1^T, s_1^T | w_1^N) \\ &= \arg \max_{N,w_1^N} p(w_1^N) \cdot \sum_{s_1^T : w_1^N} \prod_{t=1}^T p(x_t | x_1^{t-1}, s_1^t) \cdot p(s_t | x_1^{t-1}, s_1^{t-1}) \\ &= \arg \max_{N,w_1^N} p(w_1^N) \cdot \sum_{s_1^T : w_1^N} \prod_{t=1}^T p(x_t | s_t) \cdot p(s_t | s_{t-1}) \quad 1^{\text{st}} \text{ order Markov} \\ &\approx \arg \max_{N,w_1^N} p(w_1^N) \cdot \max_{s_1^T : w_1^N} \prod_{t=1}^T p(x_t | s_t) \cdot p(s_t | s_{t-1}) \quad \text{Viterbi approx.} \end{aligned}$$



Sequence Modeling and Search

Review: Hidden Markov Modeling

Discussion:

• HMM-based standard decision rule:

$$\arg \max_{N,w_1^N} p(w_1^N) \cdot \max_{s_1^T : w_1^N} \prod_{t=1}^T p(x_t | s_t) \cdot p(s_t | s_{t-1})$$

- In practice: maximum over segmentations, especially in search (Viterbi approximation)
- Ideally: sum over segmentations.
- Inconsistency for (hybrid) NN integration into acoustic model:

$$p(x_t|s) = rac{p(s|x_t) \cdot p(x_t)}{p(s)}$$

- NN provides state posterior, but state cond. probability needed.
- -p(s) approximated, e.g. [Manohar & Povey⁺ 2015].





Review: Hidden Markov Modeling

Discussion:

- Assumption of independence of acoustic context:
 - Can be relaxed by considerung window around each time frame t: $x_{t-\delta}^{t+\delta}$
 - Hybrid modeling: emission probability modelled by rescaled state posteriors $p(s|x_t)$
 - observation here appears in condition only and may be replaced by full acoustic context:
 - $\rightarrow p(s|t, x_1^T)$ (e.g. obtained by bi-directional recurrent modeling).
- Segmentation/alignment of observations to HMM states:
 - Stochastic: ideally sum over all aligments.
 - Explicit in case of Viterbi approximation: maximizing alignment.
- Integration of language model:
 - Clearly defined, can be trained separately
 - (text data vs. transcribed acoustic data).
 - However, language model scaling exponent statistically unclear.
 - Open issue: interaction of context dependence on observation and symbol/word level.





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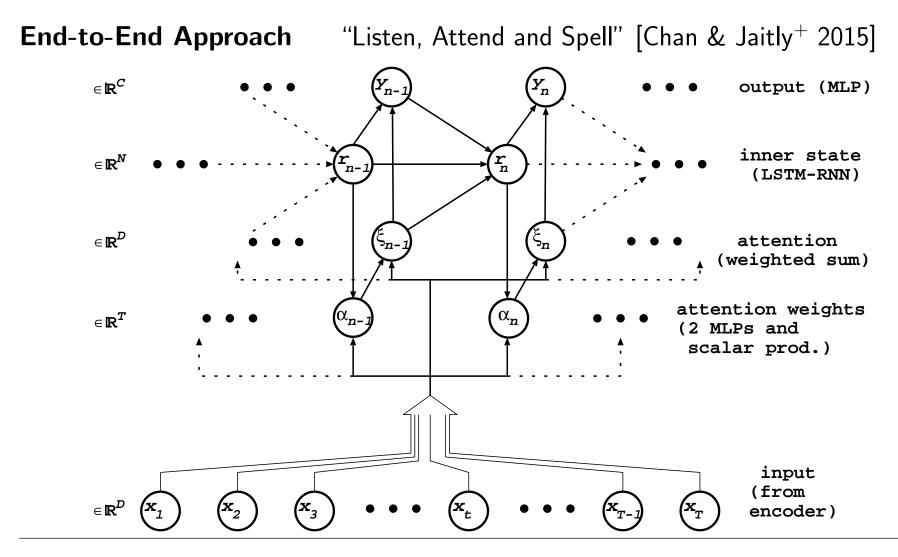


End-to-End Approach

- Motivation: End-to-end trainable neural network recognizer
 - Consistently integrate input and output sequences.
 - Does not need explicit segmentation.
 - Avoids Markov and independence assumptions.
- Sequence-to-sequence modeling [Sutskever & Vinyals⁺ 2014]:
 - Idea: separate processing of input and output into two models:
 - Encoder: Read the inputs and generate discriminative features
 - **Decoder**: Write the output symbol sequence label by label considering all encoded features
- Encoder can be viewed as non-linear transformation of input:
 - Similar to tandem in hybrid approach (hierarchical model), but:
 - Encoder output is not related to specific output labels.
 - Jointly trained within the complete end-to-end structure.



Sequence Modeling and Search





End-to-End Approach

"Listen, Attend and Spell" [Chan & Jaitly $^+$ 2015]

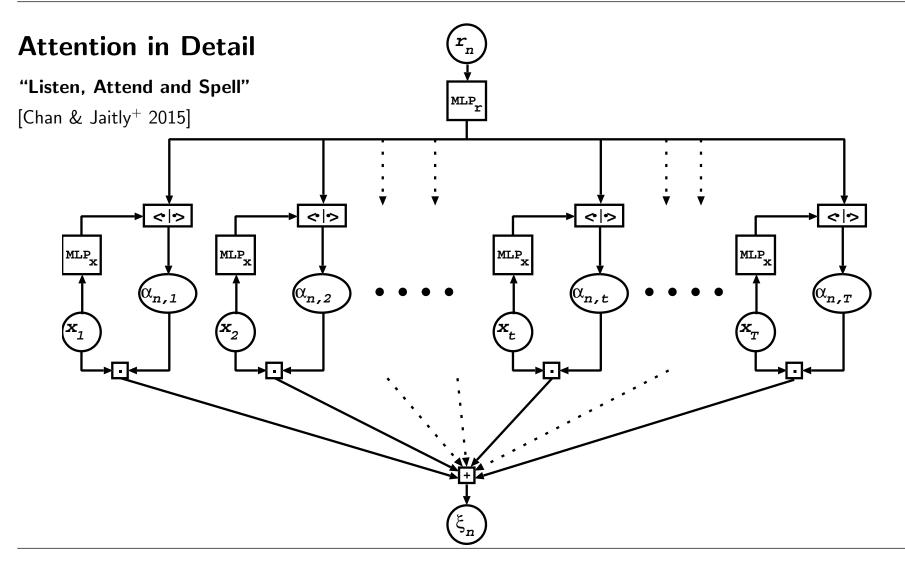
Approach:

- 1. **"Listen"**:
 - i. Encode input (bidirectional recurrent (LSTM) network, omitted in figure). Encoding usually includes gradual temporal subsampling/integration.
- 2. "Attend": at each output symbol position *n*:
 - i. Compute the current inner state value r_n from previous state r_{n-1} , output y_{n-1} , and expected input ξ_{n-1} from attention.
 - ii. Compute attention weights $\alpha_n = attend(r_n, ...)$ from current state r_n and further input (see next slide).
 - iii. Compute expected network input ξ_n as linear combination of input sequence x_1^T weighted by $\alpha_{n,1}^T$
- 3. **"Spell"**
 - i. Recurrently classify characters (symbols) from current state r_n and input ξ_n from attention.





Sequence Modeling and Search





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Discussion

- The attention process controls the segmentation
 - ightarrow (soft) alignment between symbol position and observations.
- The dependencies of the attention process still are an open research issue, choices investigated:
 - [Chan & Jaitly⁺ 2015] ("Listen, Attend and Spell"): $\alpha_n = attend(r_n, x_1^T)$
 - [Bahdanau & Chorowski⁺ 2015]: $\alpha_n = attend(r_{n-1}, y_{n-1}, \xi_{n-1})$
- Discussion:
 - No explicit alignment to specific input vectors needed.
 - However, attention is **determined** by context, i.e. it is not handled as an independent hidden stochastic variable.
 - As a consequence, suboptimal attention results (misalignments) cannot be rectified in the subsequent search process, as in HMM based modeling.



Sequence Modeling and Search

Attention Modeling Example from Handwriting

Original image en passession de mon courrier. Preprocessed image courrier. цош de possession С Ц



Sequence-to-Sequence Approach

Results: RIMES Offline Handwriting Recognition

- Input: 8×32 image slices resulting from sliding window (shift 3).
- Input layer: CNN with filter size 3 \times 3 and 64 features, no pooling.
- Hybrid: 4 BLSTM layers with 512 cells in each direction,
 - realignment: retraining on new alignment created based on hybrid.
- Attention-based: encoder (almost) equal to hybrid:
 - "subsampling" by factor of 2 after 2nd and 4th BLSTM layer (stacking) (no subsampling/stacking in framewise system).
- decoder network: single BLSTM with 512 cells for each direction.
- # params: \sim 20.8M for encoder/hybrid +700k for decoder BLSTM.

Approach	WER [%]	CER [%]
Hybrid HMM	13.0	7.6
+ realignment	12.9	5.8
Attention-based	16.2	8.0
+ LM rescoring	14.2	6.3



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Inverted Search

- Neural network based modeling provides HMM state posteriors.
- Can (sub)word sequences directly be modeled using state posteriors?
- Idea: invert alignment problem:
 - state boundaries t_1^N as hidden variables,
 - (triphone state) label sequence α_1^N directly represents word (sequence) template.
 - Approach: alternative decomposition by chain rule/Bayes identity:

$$p(\alpha_1^N | x_1^T) = \sum_{t_1^N} p(\alpha_1^N, t_1^N | x_1^T)$$

= $\sum_{t_1^N} p(\alpha_1^N | t_1^N, x_1^T) \cdot p(t_1^N | x_1^T)$
= $\sum_{t_1^N} \prod_{n=1}^N p(\alpha_n | \alpha_1^{n-1}, t_1^N, x_1^T) \cdot p(t_n | t_1^{n-1}, x_1^T)$
 $\stackrel{?}{=} \sum_{t_1^N} \prod_{n=1}^N \underbrace{p(\alpha_n | \alpha_1^{n-1}, t_{n-1}, t_n, x_1^T)}_{\text{NN-based posterior}} \cdot \underbrace{p(t_n | t_{n-1})}_{\text{length model}}$

Inverted Search

Discussion:

• inverted search, as times are aligned to triphone (state) labels, instead of vice versa.

$$p(\alpha_1^N | x_1^T) = \sum_{t_1^N} \prod_{n=1}^N \underbrace{p(\alpha_n | \alpha_1^{n-1}, t_{n-1}, t_n, x_1^T)}_{\text{NN-based posterior}} \cdot \underbrace{p(t_n | t_{n-1})}_{\text{length model}}$$

- Symbol by symbol hypothesis generation.
- Language model integrated into state posterior.

Open questions:

- How to model state posterior? not necessearily the same, as in hybrid approach: here state posterior covers multiple time frames.
- Length model? existing HMM based work less successful.
- Where are the words? word sequence determines state sequence: Effectively states represent subwords (or even words itself!).
- How to fit in (separately trained) language model?



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Specific Work

Acoustic Modeling of Raw Time Signal [Golik & Tüske⁺ 2015]

- large effort went into feature engineering for DNNs (e.g. [Seide & Li⁺ 2011, Yu & Yao⁺ 2013], ...)
- previous work [Tüske & Golik⁺ 2014] showed:
 - a simple fully connected 12-hidden-layers DNN performs well even without any feature extraction
 - WER: 22.1% (MFCC) vs. 25.5% (raw time signal)
 - first layer weights learned impulse responses of band pass filters
 - the learned filter bank roughly resembles manually defined filter bank
- convolutional neural network (CNN) is a natural tool
 - that combines learning a filter bank and acoustic modeling
- research questions:
 - how much do CNNs reduce the performance gap to hand-crafted features?
 - how can we interpret the learned weights?

Convolutional neural networks

- CNNs and were introduced about 25 years ago [LeCun & Boser $^+$ 1989]
- today: state-of-the-art in computer vision

```
([Krizhevsky & Sutskever<sup>+</sup> 2012, Jaderberg & Simonyan<sup>+</sup> 2015])
```

- applied to speech recognition tasks by [Abdel-Hamid & Mohamed⁺ 2012]: 2D filters perform convolution on a "spectrogram"
- convolution on raw time signal: 1D operation along time axis only
- output of convolutional unit *i* at position *m*:

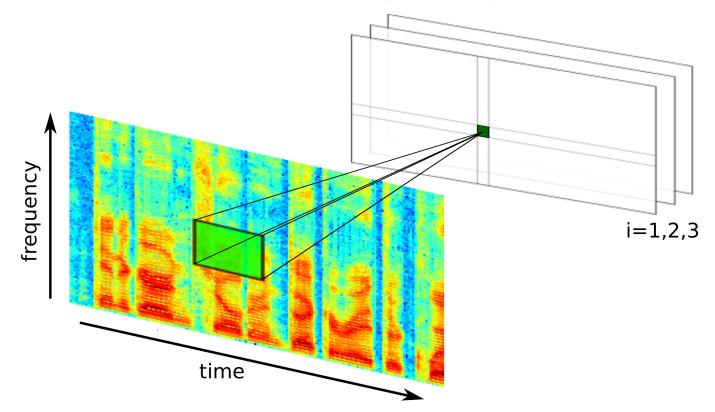
$$\mathbf{y}_{i,m} = \sigma \left(\sum_{j=m}^{m+k-1} \mathbf{w}_{i,j-m} \mathbf{x}_j + \mathbf{b}_i \right)$$

- $-x_j$ are the PCM samples
- $\{w_{i,\cdot}, b_i\}$: trainable parameters shared across all positions in the input
- -k is the length of the impulse response of a filter
- temporal sub-sampling by shifting m in steps of 32 and max pooling



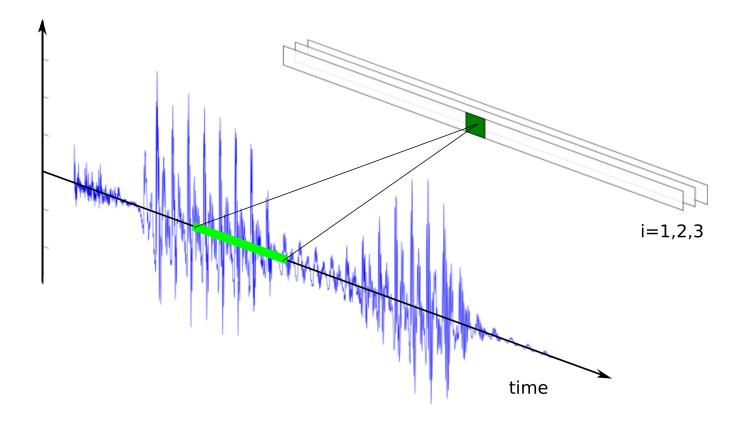
Specific Work

2D convolution in time/frequency (for ASR)





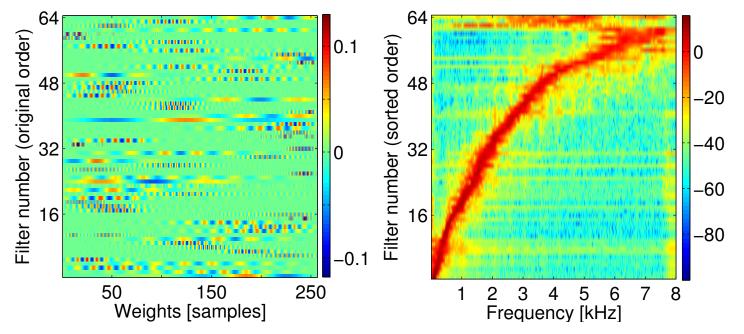
1D convolution in time only





Specific Work

Learned weights: first convolutional layer



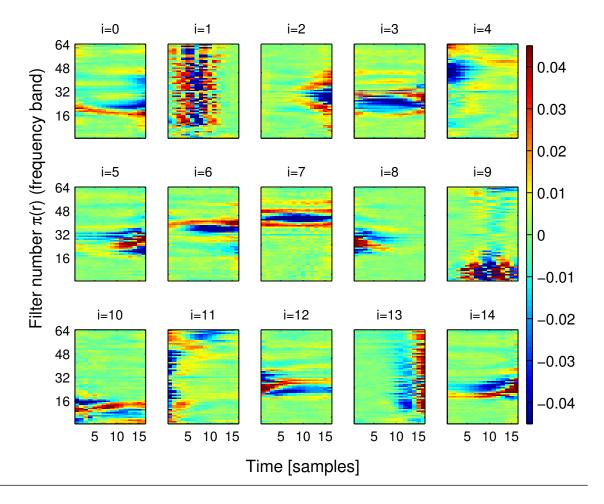
• Thus, after reordering, the output of the first convolutional layer approximates critical band energies



Specific Work

Learned weights: second convolutional layer

- reordered weights of some of the 128 filters *i* in the 2nd convolutional layer
- vertical: frequency axis, horizontal: time axis
- dynamic patterns in both time and frequency



Conclusions

- training on raw time signal works surprisingly well
- convolutional layers improve ASR performance over fully-connected layers
- the gap to MFCC's performance reduces from 15% to 6% relative WER

model	input	WER [%]
DNN	MFCC	22.1
	raw time signal	25.5
CNN		23.4

- non-stationary patterns can be captured precisely
- first and second layer weights can be interpreted as filters in time/frequency
- for sufficient amounts of training data, models trained on the raw time signal can even outperform standard preprocessing, even for multichannel scenarios [Sainath & Weiss⁺ 2015]



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Multilingual MLP Features [Tüske & Schlüter⁺ 2013]

- Exploitation of language independent information is viable:
 - Cross-lingual application of MLP features can improve performance [Stolcke & Grézl⁺ 2006].
 - Training MLP on target language usually better for similar amount of training data.
- Training MLPs on multiple languages
 - Spoken languages are based on the same speech production mechanisms.
 - Allows parameter sharing between languages.
 - Idea: share common bottleneck layer for multiple languages.
 - Robust feature: better portability to new language.
 - Exploits data available in other/multiple languages.
 - Serves as initialization prior to additional language specific training/fine-tuning.



Multilingual Bottleneck MLP

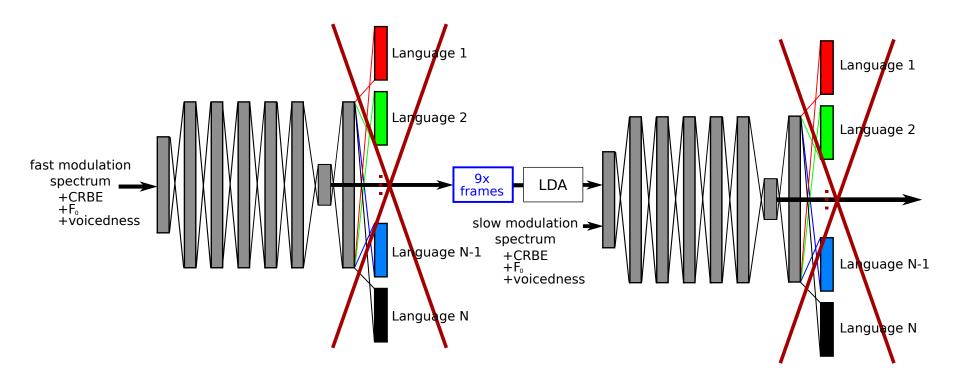
Handling multiple targets:

- Phone set incl. language id [Grézl & Karafiát⁺ 2011]:
 - NN also has to learn language identification.
- Mapping to **common phone set** [Schultz & Waibel 2001]:
 - Knowledge based (e.g IPA, SAMPA):
 - often ambiguous due to simplified lexicons.
 - Data-driven.
- Language dependent output layer [Scanzio & Laface⁺ 2008]:
 - No need to map phonetical units to common set.
 - Error back-propagation only from the active output.
 - Related to multi-task training.





Architecture of Multilingual Hierarchical Bottleneck MLP





Experiments - Quaero, Small Scale

- Experimental setup
 - Target task: French.
 - 50h of speech per language (balanced corpus size)
 - Data available for French (FR), English (EN), German (DE), Polish (PL)
 - Tandem/bottleneck approach
 - GMM: 4500 tied-states for each language
 - Shallow BN-MLPs (7000,60,7000), with phoneme targets
 - Speaker independent WER reported on Eval11
- Effect of number of languages

trai	training languages						
FR	ΕN	PL	DE	[%]			
\checkmark				22.2			
\checkmark			\checkmark	21.6			
\checkmark		\checkmark	\checkmark	21.5			
\checkmark	\checkmark	\checkmark	\checkmark	21.1			

- The more languages, the better.



Effect of Multi- and Unilingual Bottleneck Features

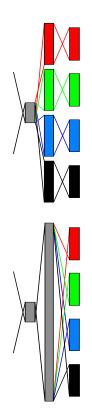
input	WER [%] for languages:						
features	FR	ΕN	DE	PL			
MFCC	25.5	31.6	25.0	18.9			
$+BN_{uni}$	22.2	26.8	21.3	15.7			
$+BN_{multi}$	21.1	24.9	20.1	15.4			

- All languages benefit from multilingual bottleneck features BN_{multi}.
- 2–5% rel. improvement over unilingual features $\mathsf{BN}_{\mathsf{multi}}.$
- 17-21% overall rel. improvement over MFCC baseline.



Experiments - Quaero, Large Scale

- Speaker adaptative training.
- Unbalanced corpus sizes for languages: 100h to 300h.
- Deep NN structure and context-dependent NN targets.
- Tuning the language dependent part of the MLP:
 - Language dependent hidden layer increases no. of parameters, but same training time last layer: huge, but **block diagonal** weight matrix (8000x6000)
 - Large, but common hidden layer increases no. of parameters even further, slower training last layer: huge full weight matrix (8000x6000)





Experiments - Quaero, Large Scale

intput features	WEF FR	R [%] † EN	for Ian DE	guages: PL
MFCC	21.6	26.4	21.4	15.9
$+BN_{uni}$	17.3	19.7	17.2	12.3
$+BN_{multi}$	17.0	19.2	16.3	12.1
+deep BN _{uni}	16.7	18.8	16.8	12.1
$+deep\;BN_{multi}$	16.2	18.1	15.7	11.7
w/lang. dep. hidden layer	16.3	18.2	15.7	11.7
w/large lang. indep. hidden layer	16.0	17.7	15.4	11.7

- Multilingual always outperform monolingual model.
- Deep structure increases margin between uni- and multilingual: relative improvement in WER: shallow BN: 2–5%, deep BN: 3–7%.
- 25–30% rel. WER impr. over speaker adaptive MFCC baseline.



Multilingual Hybrid NN: Quaero English

- Hybrid NN acoustic model with recent improvements.
 - 50 dim. gammatone input features, 17 frames context.
 - 12 hidden layers, 2000 nodes each.
 - Activation function: rectified linear units.
 - Low-rank factorized 12k output using 512 dim. linear BN.
 - WER reported on Quaero Eval corpus, 250h training data.

	Model	Criterion	WER [%]
unilingual	GMM	MPE	26.2
	hybrid NN	MPE	16.2
multilingual	hybrid NN	CE	17.3
	+fine-tuning	CE	16.7
		MPE	15.6

- Initial multilingual hybrid NN results w/o further training.
- Fine tuning: further optimization on target data.
- Still ${\sim}4\%$ rel. improvement by multilingual training.



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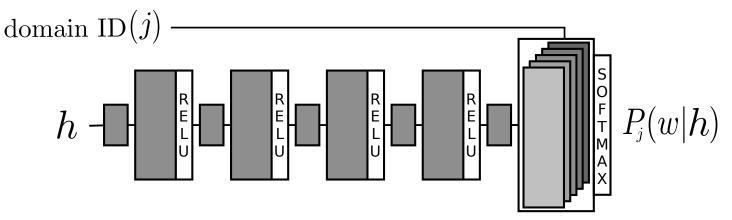


Log-Linear Interpolation of Multi-Domain Neural Network LM [Tüske & Irie⁺ 2016]

- Usual approach: linear interpolation of count LMs trained on different domains/data sets.
 - Interpolation weights optimized on target domain validation set.
 - Optimized using expectation maximization (EM) algorithm.
 - Count models are suited to be linearly combined into one single model (with union of n-grams and recomputing back-off weights)
- Goal: combination approach for neural network LMs.
 - Aiming at **single model** after interpolation of neural network LMs.
 - Linear interpolation not straightforward for NN LMs to obtain single model.
 Log-Linear combination fits better;
- Initial investigation using feed-forward NN LMs.



Joint Model



- Multiple posterior estimates
 - Active output: selected by the domain of the input vector
 - Hidden layers are shared between the domains
 - Shared vocabulary, common softmax
- Log-linear combination to obtain single overall neural network LM:
 - Leads to weighted sum of domain specific output layers.
 - Weighted sum of softmax outputs can rewritten as a single softmax output layer.





Experimental Results: Perplexities

- Training corpus: 3B words, 11 domains (Gigaword, BN/BC, TED, IWSLT, ...)
 - 50M and 2M best matching subset selected for fine-tuning
- KN 4-gram: 132.7 PPL after interpolation
- 50M LSTM-RNN: 100.5
- Retraining only multi-domain output (log-linear!) on the best BN, and interpolation: PPL 92.0

LM	multi domain	log-lin. interp.	fine-tuning 50M 2M		PPL	
50M					110.5	
JUIVI			X		109.0	
					129.0	
			X	Х	96.2	
3B	×				133.1	
	×		×	Х	95.7*	
	×	×			117.6	
	×	×	×	X	94.3	

*using the best matching output



Experimental Results: WER

- Lattice generation with count model
- Lattice rescoring using rwthlm [Sundermeyer & Alkhouli⁺ 2014]
 - Traceback lattice approximation
 - Linear-interpolation of NN LM and count LM (KN 4-gram)
- Measuring word error rate
 - Acoustic model: 12-layer multilingual BN (800h), fine tuned on 250h BN/BC target data
 - Standard Viterbi (Vi.) and confusion network (CN) decoding of the lattices

Languago Model	Dev			Eval		
Language Model		Vi.	CN	PPL	Vi.	CN
KN4	132.7	12.6	12.3	133.4	15.4	15.0
+ 50M FFNN	96.5	11.4	11.1	95.0	14.2	13.8
+ 3B, fine-tune	89.6	10.9	10.7	88.0	13.7	13.4
+ Multi-domain,log-lin,fine-tune	88.5	10.8	9.1	87.0	13.7	13.5
+ 50M LSTM	91.6	10.9	9.0	91.0	13.7	13.5



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Tandem vs. Hybrid - Integrating GMM into DNN [Tüske & Tahir⁺ 2015]

- State-of-the-art acoustic models (AM) are
 - Tandem acoustic models
 - * Gaussian Mixture Models (GMM) are trained on the output of a neural network based features
 - * Probabilistic or bottleneck (BN) tandem approach [Hermansky & Ellis⁺ 2000, Grézl & Karafiát⁺ 2007]
 - * Joint training, e.g. in [Paulik 2013]
 - Hybrid models
 - * Proposed in the early 90's [Bourlard+Morgan:1993]
 - * Estimates state posterior probabilities p(s|x) directly
 - * BN layer to train efficiently on huge number of states [Sainath & Kingsbury⁺ 2013]
- After careful optimization they show similar performance
- Goal: convert tandem into hybrid neural network representation [Tüske & Tahir⁺ 2015]
- Idea: rewrite GMM to equivalent log-linear model [Anderson 1982, Heigold & Wiesler⁺ 2010] \rightarrow softmax NN layer

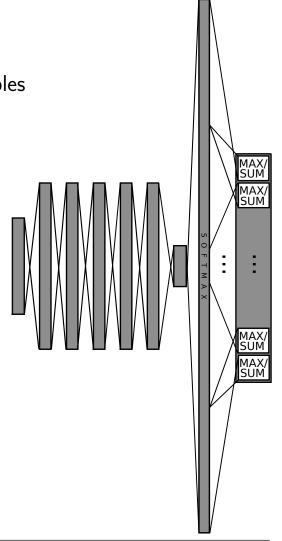


Joint GMM and Bottleneck DNN Training

- GMM with pooled covariance is a softmax layer with hidden variables
- Maximum approximation, for fast score calculation:

$$\frac{\sum_{i} \exp(w_{si}^T y + b_{si})}{Z(y)} \approx \frac{\exp(w_{s\hat{\imath}}^T y + b_{s\hat{\imath}})}{Z(y)} \bigg|_{\hat{\imath} = \operatorname*{argmax}_{i}(w_{si}^T y + b_{si})}$$

- No need for special element to implement:
 - sum- or max-pooling
- Efficient softmax is crucial (low-rank factorization; GPU)
 - GMM of 4500 states after 8 splits: \sim 1 million nodes
- Joint training of BN and GMM:
 - Maximum likelihood training of GMM on BN features
 - Convert to LMM
 - Start the joint training
- Remark: maximum approximation with given labeling (s,i) same as classical hybrid, E-M style training is also possible



Specific Work

ASR Experiments

- Task: Quaero English (250h BC/BN)
- MLP structure:
 - 12 hidden layers
 - 50 dimensional Gammatone input

System	low joint	Houtput	#param.	cnli+	critorion	WER [%]		
	rank	training	#output	₩param.	spirt	CITEMON	dev	eval
Hybrid	no		4.5k	54.7M			13.3	18.1
	yes		4.5K	49.0M	_	CE	13.5	18.2
			12.0k	52.8M			13.0	17.7
BN tandem		no	4.5k	613.0M	8	ML	14.2	19.0
		yes	4.JK	83.5M	4	CE	13.1	17.8

- Same results with less tied-triphone states
- Smaller lexical prefix-tree





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Statistical approach

- four key ingredients:
 - choice of performance measure: errors at string, word, phoneme, frame level
 - probabilistic models at these levels and the interaction between these levels
 - training criterion along with an optimization algorithm
 - Bayes decision rule along with an efficient implementation
- about recent work on artificial neural nets (2009-15):
 - significant improvements by deep MLPs and LSTM-RNNs
 - they provide one more type of probabilistic models
- long-term research topics at RWTH:
 - training criteria and error rates (at frame, phoneme, word, sentence levels)
 - open lexicon ASR: any letter sequence can be recognized
 - (fully) unsupervised training: without any transcribed training data



Future Challenges

- specific future challenges for statistical approach (incl. NNs) in general:
 - complex mathematical model that is difficult to analyze
 - questions: can we find suitable mathematical approximations with more explicit descriptions of the dependencies and level interactions and of the performance criterion (error rate)?
- specific challenges for artificial neural networks:
 - methods with better convergence?
 - can the HMM-based alignment mechanism be replaced?
 - can we find NNs with more explicit probabilistic structures?



Questions and Interpretations

- Do the NNs discover dependencies that we cannot model explicitly?
- Is it a better way of smoothing that makes the NN better?
- Is it the use of crossvalidation that makes NNs succesful?

• ...



Thank you for your attention

Any questions?



Outline

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